

# Phase Equilibria and Dielectric Behavior in the CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> System

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**Subsolidus phase equilibria in the CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> system at 1325°C in air have been determined. One ternary phase forms, Ca<sub>2</sub>AlNbO<sub>6</sub>, which exhibits a perovskite-related structure with 1:1 or NaCl-type ordering of Al<sup>3+</sup> and Nb<sup>5+</sup> on the B sites. Indexed X-ray powder diffraction data for this monoclinic compound are given (*P*2<sub>1</sub>/*n* (No. 11); *a* = 5.3780(1), *b* = 5.4154(1), *c* = 7.6248(2) Å, β = 89.968(2)°). The subsystem CaO–Nb<sub>2</sub>O<sub>5</sub> was reexamined at CaO contents above 70 mol% to clarify inconsistencies in the literature. Two phases were confirmed to form in this region: the polymorphic-ordered perovskite Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub>, with solid solution ranging from approximately 17 to 20.5 mol% Nb<sub>2</sub>O<sub>5</sub>, and the compound referred to as Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>, which was shown here to occur as essentially a point compound at the composition 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub>. The perovskite-related structure of the Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>-type phase was shown to be noncubic, and further studies are in progress. Capacitance methods at 1 MHz were used to determine the dielectric constants and associated temperature coefficients for eleven compounds in the CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> system. Ca<sub>2</sub>AlNbO<sub>6</sub> and Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> coexist in equilibria and were found to exhibit temperature coefficients of permittivity with opposite signs. Five compositions in the xCa<sub>2</sub>AlNbO<sub>6</sub>·(1–x)Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> system were prepared and their dielectric properties measured by dielectric resonator methods at 5–7 GHz. The relative permittivities and temperature coefficients of resonant frequency obtained for the endmembers Ca<sub>2</sub>AlNbO<sub>6</sub> and Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> were 30, –88 ppm/°C, and 45, +113 ppm/°C, respectively. Temperature compensation of the resonant frequency was obtained near *x* = 0.67 with a permittivity of 32; no solid solution was detected by X-ray powder diffraction.** © 2000 Academic Press

**Key Words:** CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub>, xCa<sub>2</sub>AlNbO<sub>6</sub>·(1–x)Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>; Ca<sub>2</sub>AlNbO<sub>6</sub>; Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>; Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub>; CaO:Nb<sub>2</sub>O<sub>5</sub>; microwave dielectric properties; phase diagram; calcium aluminum niobates; calcium niobates.

## INTRODUCTION

Dielectric oxide ceramics with high permittivity, low dielectric loss, and near-zero temperature dependence of

dielectric constant are critical elements in components such as resonators, oscillators, and filters for wireless communications (1–4). Relatively few ceramic systems are currently available with the properties needed for practical applications at various operating frequencies (5). Tantalate-based perovskite derivatives Ba<sub>3</sub>MTa<sub>2</sub>O<sub>9</sub>, with *M* = Zn or Mg (5–8), are unique in exhibiting permittivities of about 30 together with extremely low dielectric loss tangents (< 10<sup>–5</sup> at 1 GHz). The present work was motivated by the need for dielectric oxides that could serve as less costly alternatives to the tantalate systems for high-frequency, high-power resonator applications. Ternary Al<sub>2</sub>O<sub>3</sub>–Nb<sub>2</sub>O<sub>5</sub>-containing systems were selected for study (9) because the polarizability of Ta<sup>5+</sup> is intermediate<sup>1</sup> between that of Al<sup>3+</sup> and Nb<sup>5+</sup>, and because similar crystal chemistry is expected. The present report describes a systematic study of the subsolidus phase equilibria relations and dielectric properties in the CaO–Al<sub>2</sub>O<sub>3</sub>–Nb<sub>2</sub>O<sub>5</sub> system.

## Review of Prior Work

The CaO–Al<sub>2</sub>O<sub>3</sub> system has been well studied owing to its importance in structural ceramic materials (15); five binary compounds are known to form: Ca<sub>3</sub>Al<sub>2</sub>O<sub>6</sub>, Ca<sub>12</sub>Al<sub>14</sub>O<sub>33</sub> (moisture-sensitive), CaAl<sub>2</sub>O<sub>4</sub>, CaAl<sub>4</sub>O<sub>7</sub>, and CaAl<sub>12</sub>O<sub>19</sub> (16).

In several studies of the binary Al<sub>2</sub>O<sub>3</sub>–Nb<sub>2</sub>O<sub>5</sub> system (15), compounds have been reported to occur at molar ratios of 1:1, 1:9, 1:11, 1:25, and 1:49, respectively. However, the preponderance of experimental evidence suggests that only three binary compounds form at 1:1, 1:11, and 1:49 (9, 17–22).

<sup>1</sup>Although the polarizability of Ta<sup>5+</sup> given in (10) (4.73 Å<sup>3</sup>) is larger than that given for Nb<sup>5+</sup> (3.97 Å<sup>3</sup>), considerable experimental data suggest that the reverse is true (11, 12). For example, the relative permittivities of isostructural Ba<sub>3</sub>ZnTa<sub>2</sub>O<sub>9</sub> and Ba<sub>3</sub>ZnNb<sub>2</sub>O<sub>9</sub> are ~30 (5) and ~40 (13), respectively. Similarly, for Ca<sub>2</sub>AlNbO<sub>6</sub> and Ca<sub>2</sub>AlTaO<sub>6</sub> the respective values are 25 and 20 (14).



The CaO–Nb<sub>2</sub>O<sub>5</sub> binary system has been the least studied with some variability in reported results (15). Three equilibrium phases, Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>, Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub>, and CaNb<sub>2</sub>O<sub>6</sub>, were indicated in the earliest published phase diagram (23). A later study (24) indicated Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub> and CaNb<sub>2</sub>O<sub>6</sub> as equilibrium phases, in addition to three “Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub>-type” solid solution phases; the authors did not report the existence of Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>. Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub> and CaNb<sub>2</sub>O<sub>6</sub> have been well characterized; the former occurs with a monoclinic perovskite-slab-type structure (25–27), and the latter adopts a columbite-type structure (28–30). The polymorphic perovskite derivative Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub> has recently been characterized in detail (31, 32). This compound exhibits four structures with different Ca and Nb ordering on the B-cation sites. The phases include a low-temperature 2:1 ordering ( $T < 1400^{\circ}\text{C}$ ), a metastable “3:1” ordering ( $T < 1400^{\circ}\text{C}$ ), and two high-temperature forms with 1:1 NaCl-like ordering ( $T > 1400^{\circ}\text{C}$ ). The highest-temperature polymorph without octahedral tilting can only be distinguished by a change in microstructure of specimens quenched from  $T > 1500^{\circ}\text{C}$ .

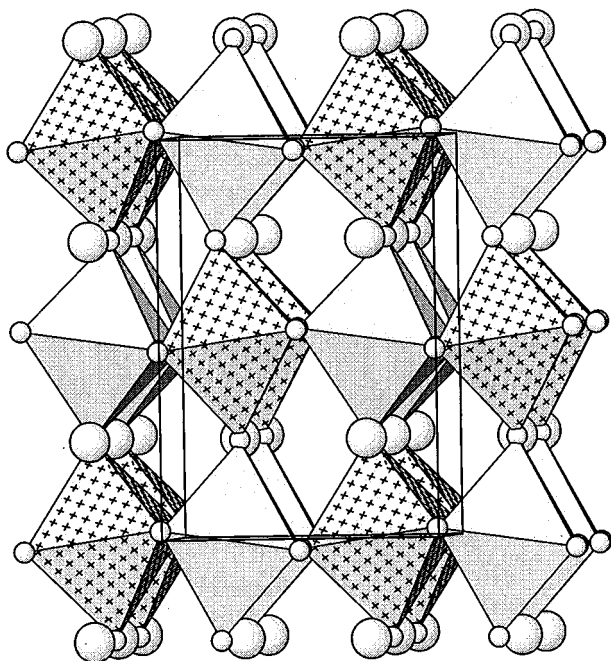
Reports describing the compound Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> are variable. Initially, this phase was reported as an incongruently melting ( $1560^{\circ}\text{C}$ ) perovskite derivative with two polymorphs, referred to as cubic “Type I” and a “Type II” (23). The authors indexed the X-ray powder pattern for Type I with a unit cell of  $a = 23.934 \text{ \AA}$ , and stated that “it satisfies

the vast majority of the faint lines” (23). Subsequent work from the same laboratory showed that Type II was actually one of the Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub> polymorphs, and reported a phase diagram that does not contain Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> (24). Later studies using electron and X-ray diffraction concluded that Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> forms with a tetragonal perovskite-related cell ( $a = 16.90 \text{ \AA} \approx 3\sqrt{2}a_c$ ,  $c = 23.73 \text{ \AA} \approx 6a_c$ ,  $P4/nmc$ , where  $a_c = 4 \text{ \AA}$  for cubic perovskite) (33); however, these authors concluded that the phase is oxygen deficient, i.e., Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8-x</sub>. An X-ray powder diffraction pattern was given (33) with indices based on this tetragonal cell, which accounted for observed peaks not allowed by the cubic  $23.934\text{-\AA}$  cell reported earlier (23).

The ternary compound Ca<sub>2</sub>AlNbO<sub>6</sub> was described in 1965 (34) as a perovskite derivative with an orthorhombic superstructure ( $a = 5.38 \text{ \AA} \approx \sqrt{2}a_c$ ,  $b = 5.40 \text{ \AA} \approx \sqrt{2}a_c$ ,  $c = 7.61 \text{ \AA} \approx 2a_c$ ; X-ray powder data) arising from ordering of Al<sup>3+</sup> and Nb<sup>5+</sup> on the octahedral B sites. Ca<sub>2</sub>AlNbO<sub>6</sub> reportedly melts congruently at  $1675^{\circ}\text{C}$  (35), and its dielectric behavior has been characterized at gigahertz frequencies ( $\epsilon_r = 25$ ,  $Qxf = 7500 \text{ GHz}$ ,  $\tau_f = -87 \text{ ppm}^{\circ}\text{C}$ ) (14). The structure of Ca<sub>2</sub>AlNbO<sub>6</sub> is illustrated in Fig. 1. The arrangement is very similar to that in CaTiO<sub>3</sub> (36), with 1:1 or NaCl-like ordering of Al<sup>3+</sup> and Nb<sup>5+</sup> superimposed on octahedral tilting.

## EXPERIMENTAL METHODS

Specimens were prepared by solid-state reaction of CaCO<sub>3</sub> (99.999%), Al<sub>2</sub>O<sub>3</sub> (0.3 μm, 99.99%) and Nb<sub>2</sub>O<sub>5</sub> (optical grade). Prior to each heat treatment, samples were ground with an agate mortar and pestle for 15 min, pelletized, and placed on sacrificial powder of the same composition in a Pt-foil-lined alumina combustion boat. After an initial overnight calcine at  $950^{\circ}\text{C}$ , multiple 2–4 day heatings (with intermediate grinding and repelletizing) were carried out in the temperature range  $1300\text{--}1400^{\circ}\text{C}$ ,  $25\text{--}50^{\circ}\text{C}$  below the solidus temperatures that had been previously determined by melting point experiments; samples were furnace-cooled to  $\sim 750^{\circ}\text{C}$  and then air-quenched on the benchtop. The minimum solidus temperature observed in the ternary system was  $\sim 1350^{\circ}\text{C}$ , for the composition 0.20:0.20:0.60 CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub>. Typically, three to six heatings were required to attain equilibrium, which was presumed when no further changes could be detected in the weakest peaks observed in the X-ray powder diffraction patterns. Phase relations determined in this manner were reconfirmed by annealing specimens at  $1325^{\circ}\text{C}$  followed by water quenching. Quenching, melting point, and crystal-growth experiments were carried out in sealed Pt capsules. The colors of the polycrystalline specimens ranged from white to light tan. Single crystals of the Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>-type phase were grown from a flux of 3CaO:V<sub>2</sub>O<sub>5</sub> at a 50:50 wt.% mixture of equilibrated Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> powder and flux.



**FIG. 1.** The structure of the perovskite derivative Ca<sub>2</sub>AlNbO<sub>6</sub>. Large spheres denote Ca<sup>2+</sup>, small spheres, oxygen; stippled and gray octahedra represent the 1:1 or NaCl-like ordered Al<sup>3+</sup> and Nb<sup>5+</sup> sites. The arrangement is very similar to that in CaTiO<sub>3</sub>, with a slight monoclinic distortion (36).

The mixture was annealed for 2 h at 1475°C, cooled at 1°C/h to 1300°C, and removed from the furnace. Pale yellow crystals exhibiting glassy fracture were harvested from the reaction mass by leaching with dilute hydrochloric acid. Attempts to grow crystals of  $\text{Ca}_3\text{Nb}_2\text{O}_8$  using neat charges slow-cooled from 1575°C were not successful, nor were experiments carried out at 1200°C using NaCl as a flux.

Phase assemblages were ascertained from X-ray powder diffraction data, which were obtained with a Philips<sup>2</sup> diffractometer equipped with incident Soller slits,  $\theta$ -compensating slit, a graphite monochromator, and a scintillation detector. Samples were mounted in well-glass slides. Routine identification patterns were collected at ambient temperatures using  $\text{CuK}\alpha$  radiation with a  $0.02^\circ 2\theta$  step size and a 2-s count time. For  $\text{Ca}_2\text{AlNbO}_6$ , a longer scan was taken ( $0.010^\circ 2\theta$  step size, 5 s count time) to obtain data for least-squares refinement of lattice parameters. Intensity data (measured as relative peak heights above background) of hand-picked peaks were obtained using the Siemens DIFFRAC5000 second-derivative peak locate program. The observed  $2\theta$  line positions reported here for  $\text{Ca}_2\text{AlNbO}_6$  have been corrected using SRM 660,  $\text{LaB}_6$  (37) as an external calibrant. Lattice parameters were refined using the corrected powder diffraction data ( $2\theta$  values,  $\text{CuK}\alpha_1 = 1.540562 \text{ \AA}$ ) with the least-squares program CELLSVD (38). During the refinement, the indices of unequivocally indexed reflections were fixed in accordance with the powder pattern calculated using the GSAS package (39) and the positional parameters reported by Levin *et al.*, from a neutron powder diffraction study of the  $\text{Ca}_2\text{AlNbO}_6$ - $\text{CaTiO}_3$  system (36). For the  $\text{Ca}_3\text{Nb}_2\text{O}_8$ -type phase, high-resolution X-ray powder data were collected using a Siemens D5000 diffractometer equipped with a focusing Ge incident beam monochromator, a sample spinner, and a scanning position-sensitive detector (PSD). The scan range was from  $15^\circ$  to  $155^\circ 2\theta$ . Single crystals were characterized by the precession camera method using Zr-filtered  $\text{MoK}\alpha$  radiation.

Dielectric properties were evaluated by capacitance methods at 1 MHz using cylindrical pellets (diameters 8–9 mm) pressed from equilibrated powders, sintered  $\sim 50^\circ\text{C}$  below the solidus temperatures, and then polished to a height of approximately 1.5 mm. Sample density ( $\rho_{\text{obs}}$ ) was estimated from the mass and dimensions of the pellets and compared to the crystallographic density ( $\rho_{\text{calc}}$ ) to estimate pore volume. Electrodes were formed by thermally evaporating approximately 25 nm of Cr followed by 300 nm of Au onto an 8.0-mm circular area on the cylinder faces in order to form parallel plate capacitors. Au wires were attached to each electrode and to Pt wires leading to an

HP4194A Impedance Analyzer. All contacts were made with Ag paint. Variable-temperature data were obtained by heating the capacitors in a box furnace; specimen temperature was measured by a case-grounded K-type thermocouple located under the capacitor. The lead-compensated capacitance was measured with the impedance analyzer in the frequency range 100 Hz to 10 MHz, with an oscillator amplitude of 0.5 V, while the temperature decreased from 200 to 25°C over  $\sim 15$  h, with the furnace power off. The capacitance at 25°C and its temperature coefficient were determined from a linear regression of the 1-MHz data taken over the range 25 to 100°C. Both quantities were corrected for edge effects (40) and used to calculate the observed dielectric constant  $\epsilon_{\text{obs}}$  and its temperature coefficient, which were then corrected for porosity using the Bruggeman effective medium theory (41) to give  $\epsilon_{\text{corr}}$  and  $\tau_\epsilon$ . The uncertainty in the dielectric constants and their temperature coefficients is  $\pm 20\%$  and is mainly attributed to imprecise overlap of the electrodes on each side of the capacitor.

The dielectric properties of five specimens along the composition line  $\text{Ca}_2\text{AlNbO}_6$ - $\text{Ca}_3\text{Nb}_2\text{O}_8$  were evaluated at microwave frequencies (5–8 GHz) using cylindrical pellets (diameters and heights 8–9 mm) that has been pressed from equilibrated powders, sintered at 1475°, and polished. Samples were measured as  $\text{TE}_{011}$  or  $\text{TE}_{07\delta}$  dielectric resonators in a parallel plate waveguide using the Hakki-Coleman or Courtney (42, 43), or modified Courtney (44, 45) techniques. Variable-temperature data were obtained at six temperatures between 20 and 100°C using the specimen as a  $\text{TE}_{011}$  dielectric resonator situated internally in a cylindrical cavity. Relative real permittivity ( $\epsilon'_r$ ) was calculated from the measured frequency of the  $\text{TE}_{011}$  or  $\text{TE}_{07\delta}$  resonance mode and sample dimensions; loss tangent ( $\tan \delta$ ) was determined from the measured system unloaded  $Q$  factor. For all results reported, variable-temperature and variable-frequency conductor losses were measured and accounted for. The temperature coefficient of resonant frequency ( $\tau_f$ ) was calculated from a linear regression analysis of the data obtained at different temperatures. The quality factor  $Q$  was calculated as  $(\tan \delta)^{-1}$ . Permittivity and dielectric loss tangent values were corrected to theoretical density using effective-medium theory (46, 47). The uncertainties in the reported permittivity values are approximately  $\pm 10\%$ , and are dominated by the estimate of pore volume. The estimated uncertainty in measurement of loss tangent is  $2 \times 10^{-5}$ .

## RESULTS AND DISCUSSION

### *CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> System*

The subsolidus phase equilibria relations found in the present study are shown in Fig. 2 along with the dielectric constant, and the sign of its temperature dependence, for selected compounds. Only one ternary compound,

<sup>2</sup>Certain commercial equipment is identified in order to adequately specify the experimental procedure; recommendation or endorsement by the National Institute of Standards and Technology is not therein implied.

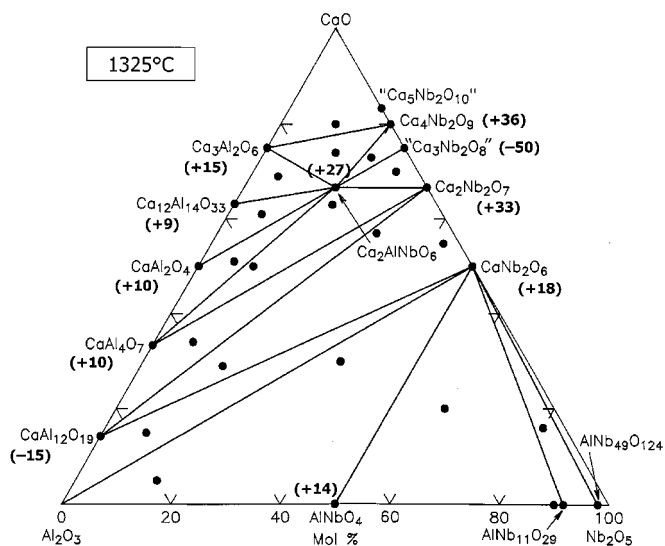


FIG. 2. Subsidiary phase equilibria relations found in the CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> system in air. The dielectric constants ( $\epsilon_{\text{corr}}$ ) and the signs of their temperature dependences ( $\tau_\epsilon$ ) are included for selected compounds (Table 2). Ca<sub>2</sub>AlNbO<sub>6</sub> and Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> occur in equilibrium with each other and exhibit opposite signs of  $\tau_\epsilon$ .

Ca<sub>2</sub>AlNbO<sub>6</sub>, was found to occur. Powder diffraction data for this compound are given in Table 1 and have been indexed on the basis of a monoclinic unit cell ( $P2_1/n$  (No. 11);  $a = 5.3780(1)$ ,  $b = 5.4154(1)$ ,  $c = 7.6248(2)$  Å,  $\beta = 89.968(2)^\circ$ ) (36), which is very similar to the CaTiO<sub>3</sub>-like orthorhombic cell reported in earlier work (34).

In contrast to the analogous systems SrO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> (9) and BaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> (49), the tetragonal tungsten bronze (TTB) structure was not observed to form in the CaO-containing ternary: a specimen with nominal composition Ca<sub>6</sub>AlNb<sub>9</sub>O<sub>30</sub>, equilibrated within 20°C of the solidus (1425°C), yielded a 3-phase mixture of Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub>, CaNb<sub>2</sub>O<sub>6</sub>, and CaAl<sub>12</sub>O<sub>19</sub>. This observation is consistent with the narrow region of stability of the TTB structure in the SrO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> system—the structure is destabilized upon proceeding to the smaller Ca<sup>2+</sup> ion. In the present study, X-ray powder diffraction data indicated no evidence of solid solution formation around the compound AlNbO<sub>4</sub>, as was reported in a study of the MgO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> system (50).

The observed and corrected dielectric constants ( $\epsilon_{\text{obs}}$  and  $\epsilon_{\text{corr}}$ ) and their corrected temperature coefficients ( $\tau_\epsilon$ ) for selected compositions in the CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> system are given in Table 2. Positive temperature coefficients of permittivity were observed for most of the compositions, while negative values were obtained for CaAl<sub>12</sub>O<sub>19</sub> and Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>. The Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub> sample was a mixture of polymorphic forms, which are known to exhibit differences in dielectric properties (32). The temperature dependence of the permittivity of Ca<sub>2</sub>AlNbO<sub>6</sub> is opposite in sign and similar in magnitude to that of Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>, as shown in

TABLE 1  
X-Ray Powder Diffraction Data for Ca<sub>2</sub>AlNbO<sub>6</sub>

<i>h</i>	<i>k</i>	<i>l</i>	$2\theta_{\text{obs}}$	$I_{\text{obs}}$	$2\theta_{\text{calc}}$	$\Delta 2\theta$	$d_{\text{obs}}$
0	1	1	20.101	14	20.095	0.006	4.4138
1	0	1			20.184		
-1	0	1			20.194		
1	1	0	23.303	18	23.313	-0.010	3.8140
0	0	2			26.075		
1	1	1	33.033	47	33.055	-0.022	2.7094
0	2	0			33.183		
1	1	2	33.192	100	33.196	-0.004	2.6968
-1	1	2			33.277		
2	0	0	35.128	1	35.141	-0.013	2.5525
0	2	1			37.144		
1	2	0	37.300	1	37.305	-0.005	2.4087
2	1	0			39.167		
1	0	3	40.834	2	40.843	-0.009	2.2080
0	2	2			42.709		
1	1	3	44.332	1	44.323	0.009	2.0416
-1	2	2			47.634		
2	2	0	47.668	2	49.180	-0.017	1.8516
0	0	4			52.161		
2	2	1	52.301	6	52.300	0.001	1.7477
1	2	3			52.380		
3	0	1	53.516	6	53.502	0.014	1.7108
1	3	0			53.664		
2	2	2	53.679	10	53.683	-0.004	1.7060
-2	2	2			53.697		
1	1	4	54.930	2	54.941	-0.011	1.6701
-1	1	4			55.273		
1	3	1	59.153	33	59.121	0.023	1.5605
-1	3	2			59.414		
3	1	2	59.440	1	62.025	0.001	1.4950
-3	1	2			63.185		
2	1	4	63.352	5	63.350	0.002	1.4668
2	3	1			65.708		
-1	0	5	65.904	1	65.896	0.008	1.4161
1	3	3			69.360		
1	1	5	69.671	28	69.684	-0.013	1.3484
0	4	0			69.882		
2	2	4	70.577	1	70.599	-0.022	1.3333
4	0	0			71.832		
0	4	1	72.380	1	72.358	0.022	1.3045
1	4	0			73.088		
-1	4	1	73.333	4	73.341	-0.008	1.2899
1	3	4			73.477		
-2	1	5	73.579	3	73.573	0.006	1.2862
4	1	1			74.279		
0	4	2	74.435	3	74.434	0.001	1.2735
1	3	4			74.449		
-1	3	4	74.676	2	74.688	-0.012	1.2700
3	1	4			75.778		
-3	3	1	77.212	1	77.222	-0.010	1.2345
-4	1	2			79.138		
2	4	0	79.371	18	79.332	0.016	1.2062
3	3	2			79.355		

TABLE 1— Continued

<i>h</i>	<i>k</i>	<i>l</i>	$2\theta_{\text{obs}}$	$I_{\text{obs}}$	$2\theta_{\text{calc}}$	$\Delta 2\theta$	$d_{\text{obs}}$
4	2	0	79.530	9	79.532	-0.002	1.2042
0	4	3	80.297	1	80.277	0.020	1.1946
2	2	5	80.564	1	80.557	0.007	1.1913
-1	4	3	82.672	1	82.660	0.012	1.1662
-4	1	3	83.180	1	83.166	0.014	1.1604
2	4	2	83.840	1	83.860	-0.020	1.1529
4	2	2	84.240	1	84.244	-0.004	1.1485
-1	3	5	85.181	1	85.161	0.020	1.1382
-3	1	5	85.430	1	85.439	-0.009	1.1355
0	4	4	88.493	6	88.510	-0.017	1.1039
4	0	4			88.999		
-4	0	4	89.041	3	89.058	-0.017	1.0985
-1	0	7	92.378	2	92.372	0.006	1.0674
5	0	1	92.628	1	92.635	-0.007	1.0652
3	3	4	93.436	1	93.418	0.018	1.0581
5	1	0	93.776	1	93.795	-0.019	1.0551
1	5	1	94.162	1	94.186	-0.024	1.0518
3	4	2	95.631	1	95.632	-0.001	1.0395
1	5	2	97.693	5	97.712	-0.019	1.0230
1	3	6	98.019	5	98.037	-0.018	1.0204
-3	1	6	98.332	12	98.343	-0.011	1.0180
-5	1	2	98.526	7	98.520	0.006	1.0165
0	5	3	101.257	1	101.262	-0.005	0.9964
2	1	7	101.791	2	101.787	0.004	0.9926
4	1	5	101.911	2	101.921	-0.010	0.9917
1	5	3	103.648	1	103.664	-0.016	0.9798
4	4	0	107.710	3	107.691	0.019	0.9538
4	4	1	108.922	1	108.915	0.007	0.9466
1	5	4	112.282	1	112.276	0.006	0.9275
-1	5	4			112.292		
4	4	2			112.660		
-4	4	2	112.716	1	112.692	0.024	0.9252
0	6	0	117.160	1	117.173	-0.013	0.9026
3	5	2	117.538	6	117.536	0.002	0.9008
-3	5	2			117.560		
-3	3	6	117.968	7	117.957	0.011	0.8987
1	6	1	121.191	1	121.205	-0.014	0.8841
-2	3	7	121.949	1	121.930	0.019	0.8809
6	1	1	122.512	1	122.529	-0.017	0.8785
2	4	6	123.081	1	123.089	-0.008	0.8761
4	2	6	123.550	1	123.528	0.022	0.8742
1	5	5	124.235	1	124.245	-0.010	0.8714
2	6	0	128.370	2	128.375	-0.005	0.8556
4	4	4			129.046		
-4	4	4	129.137	8	129.122	0.015	0.8529
2	2	8			129.180		
-2	2	8			129.256		
6	2	0	129.730	2	129.710	0.020	0.8508
1	4	7	133.503	1	133.501	0.002	0.8383
-6	1	3	134.553	6	134.570	-0.017	0.8351
3	5	4			134.995		
-3	5	4	135.080	1	135.057	0.023	0.8335
3	1	8	135.676	1	135.665	0.011	0.8317

Note.  $P2_1/n$  (No. 11);  $a = 5.3780(1)$ ,  $b = 5.4154(1)$ ,  $c = 7.6248(2)$  Å;  $\beta = 89.968(2)^\circ$  (Figure of merit (48):  $F(90) = 18.7(0.0116, 414)$ ).

Fig. 3. Since these compounds were found to occur in equilibrium with each other (Fig. 2), a temperature-compensated, thermodynamically stable mixture was expected to form on the  $\text{Ca}_2\text{AlNbO}_6$ - $\text{Ca}_3\text{Nb}_2\text{O}_8$  join.

Five specimens were prepared in the  $x\text{Ca}_2\text{AlNbO}_6 \cdot (1-x)\text{Ca}_3\text{Nb}_2\text{O}_8$  system with  $x$  values 0.0, 0.25, 0.50, 0.75, and 1.0. No solid solution formation was detectable by X-ray powder diffraction. The dielectric properties obtained for these compositions at microwave frequencies are given in Table 3. Figure 4 shows the relative real permittivity ( $\epsilon'_{r,\text{obs}}$ ) and temperature coefficient of resonant frequency ( $\tau_f$ ) as a function of  $x$  value. The temperature-compensated mixture occurs near  $x = 0.67$  with a corrected permittivity of  $\sim 32$ —the expected  $Qxf$  product (@7 GHz) is on the order of 10,000 GHz (Table 3); however, this value should be considered a minimum since the specimens were not fully dense, and those with  $x < 1$  contained a small amount of  $\text{Ca}_2\text{Nb}_2\text{O}_7$ . The properties for pure  $\text{Ca}_2\text{AlNbO}_6$  obtained here are similar to those reported by Kagata and Kato ( $\epsilon_r = 25$ ,  $\tau_f = -87$  ppm/ $^\circ\text{C}$ ) (14), except for a higher  $Qxf$  product (14,000 vs 7500 GHz).

#### *CaO:Nb<sub>2</sub>O<sub>5</sub> System*

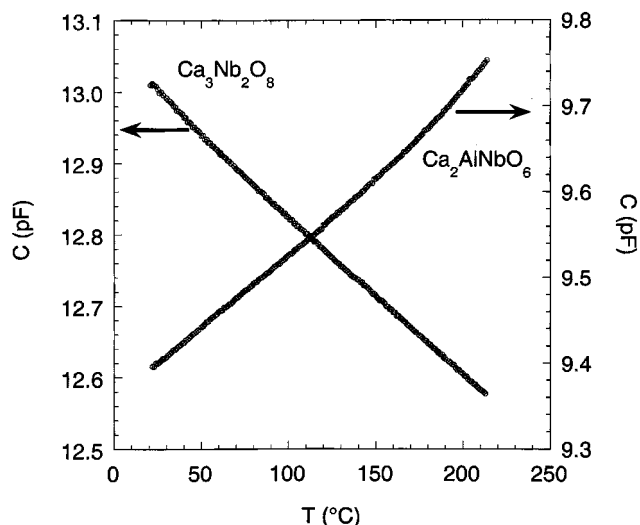
The results obtained here for the binary system at calcia contents above 70 mol% are shown in Fig. 5. The perovskite derivative  $\text{Ca}_4\text{Nb}_2\text{O}_9$  exhibited solid solution ranging from approximately 17 to 20.5 mol%  $\text{Nb}_2\text{O}_5$ . At  $\text{Ca}_4\text{Nb}_2\text{O}_9$ , the phase transition between the 2:1 and 1:1 ordered polymorphs (31, 32) was observed by X-ray diffraction to occur between specimens quenched from 1400 and 1450 $^\circ\text{C}$ . For the specimens in the 2-phase region between the  $\text{Ca}_4\text{Nb}_2\text{O}_9$  solid solution and CaO, the phase transition was found to occur at approximately 1375 $^\circ\text{C}$  as shown in the phase diagram (Fig. 5). At 21 mol%  $\text{Nb}_2\text{O}_5$ , the metastable “3:1” (or “ $\text{LT}_{1/4}$ ” (31, 32)) ordered polymorph of  $\text{Ca}_4\text{Nb}_2\text{O}_9$  was found to be stable between 1375 and 1575 $^\circ\text{C}$ .

TABLE 2

Sample Density ( $\rho$ ), Observed and Corrected Dielectric Constants ( $\epsilon_{\text{obs}}$  and  $\epsilon_{\text{corr}}$ ), and Corrected Temperature Coefficient of Permittivity ( $\tau_\epsilon$ ) for Selected Compounds Found in the  $\text{CaO-Al}_2\text{O}_3$ - $\text{Nb}_2\text{O}_5$  System

Composition	$\rho$ (%)	$\epsilon_{\text{obs}}$	$\epsilon_{\text{corr}}$	$\tau_\epsilon$ (ppm/ $^\circ\text{C}$ )
$\text{Ca}_2\text{AlNbO}_6$	93	25	27	170
$\text{Ca}_4\text{Nb}_2\text{O}_9$	84	28	36	19
$\text{Ca}_3\text{Nb}_2\text{O}_8$	82	37	50	-135
$\text{Ca}_2\text{Nb}_2\text{O}_7$	90	29	33	320
$\text{CaNb}_2\text{O}_6$	90	16	18	83
$\text{CaAl}_4\text{O}_7$	91	9	10	175
$\text{Ca}_3\text{Al}_2\text{O}_6$	93	14	15	776
$\text{Ca}_{12}\text{Al}_{14}\text{O}_{33}$	93	8	9	1644
$\text{CaAl}_2\text{O}_4$	90	8	10	124
$\text{CaAl}_{12}\text{O}_{19}$	76	10	15	-247
$\text{AlNbO}_4$	92	12	14	123

Note. Capacitance measurements, 1 MHz, 25 $^\circ\text{C}$ .



**FIG. 3.** Capacitance as a function of temperature for  $\text{Ca}_3\text{Nb}_2\text{O}_8$  and  $\text{Ca}_2\text{AlNbO}_6$ . The temperature coefficients are opposite in sign and similar in magnitude.

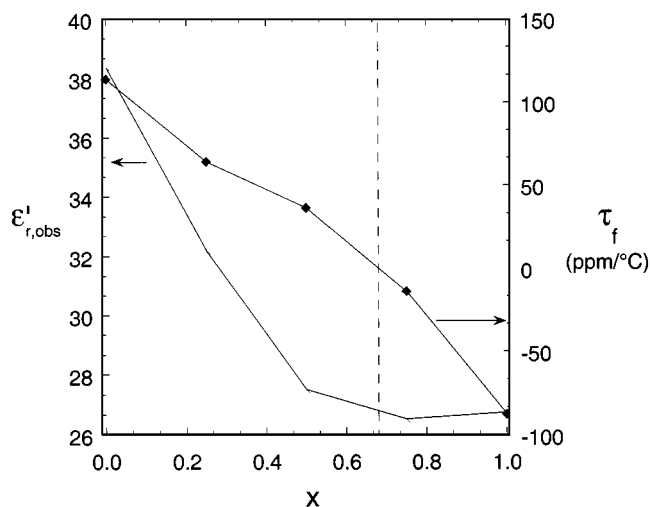
Interestingly, the phase referred to as  $\text{Ca}_3\text{Nb}_2\text{O}_8$  was found to occur with little or no solid solution at the composition 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub>—stoichiometric specimens at  $\text{Ca}_3\text{Nb}_2\text{O}_8$  (= 75:25 CaO:Nb<sub>2</sub>O<sub>5</sub>) always exhibited a small amount of  $\text{Ca}_2\text{Nb}_2\text{O}_7$  in the X-ray powder diffraction patterns, despite repeated annealing at 1450°C. Closely spaced specimens were prepared in order to determine the composition at which “ $\text{Ca}_3\text{Nb}_2\text{O}_8$ ” occurs as a single phase. As shown in Fig. 6, compositions on either side of 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub> exhibit traces of the expected neighboring binary phases. The  $\text{Ca}_3\text{Nb}_2\text{O}_8$ -type phase begins to decompose above 1475°C; thus, previously reported

**TABLE 3**  
Dielectric Properties of  $x\text{Ca}_2\text{AlNbO}_6:(1-x)\text{Ca}_3\text{Nb}_2\text{O}_8$  Mixtures<sup>a</sup>

$x$	$\rho$ %	$\epsilon'_{r,\text{obs}}$	$\epsilon'_{r,\text{corr}}$	$f$ (GHz)	$\tau_f$ (ppm/°C)	$\tan \delta$	$Q_{xf}$ (GHz)
0.000	88	38	45	5.8886	+113	$8.3 \times 10^{-4}$	7100
0.250	87	32	40	6.3387	+64	$8.5 \times 10^{-4}$	7500
0.500	83	28	36	6.8567	+36	$7.7 \times 10^{-4}$	8900
0.750	88	26	32	6.9750	-14	$5.3 \times 10^{-4}$	13,200
1.000	93	27	30	7.0163	-88	$5.0 \times 10^{-4}$	14,000

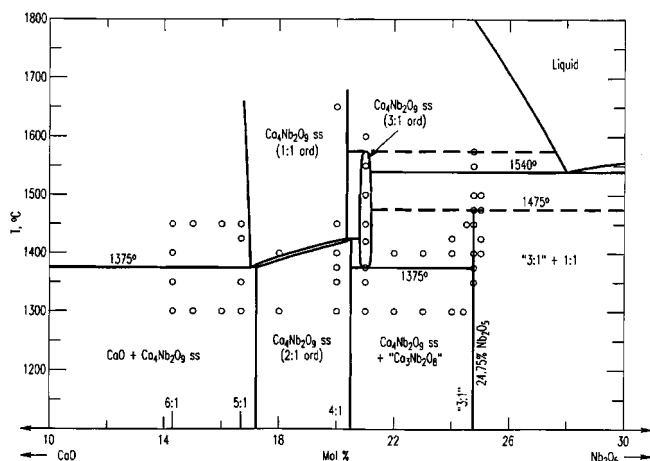
Note. Dielectric resonator measurements, 30°C.

<sup>a</sup>The compound  $\text{Ca}_3\text{Nb}_2\text{O}_8$  was later found to occur as a single phase at the composition 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub>; therefore, the  $x\text{Ca}_2\text{AlNbO}_6:(1-x)\text{Ca}_3\text{Nb}_2\text{O}_8$  specimens with  $x < 1$  actually contain from 1 to 4 mol%  $\text{Ca}_2\text{Nb}_2\text{O}_7$ , respectively, as a third phase. The dielectric properties obtained for single-phase “ $\text{Ca}_3\text{Nb}_2\text{O}_8$ ” at 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub> are  $\rho = 90\%$ ,  $\epsilon'_{r,\text{obs}} = 35$ ,  $\epsilon'_{r,\text{corr}} = 41$ ,  $f = 8.6583$  GHz,  $\tau_f = +123$  ppm/°C,  $\tan \delta = 1.0 \times 10^{-3}$ ,  $Q_{xf} = 8700$  GHz.

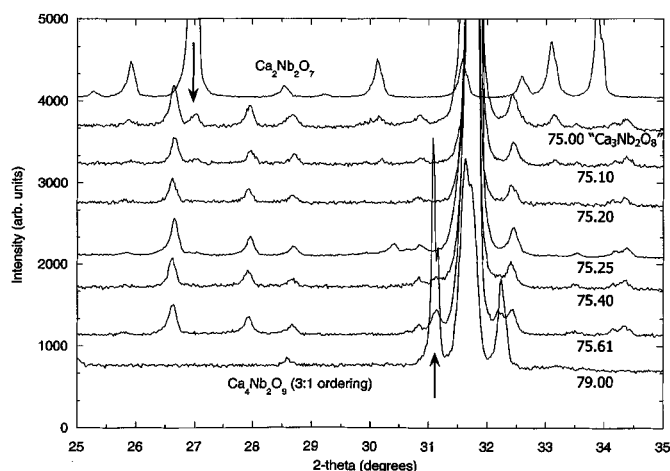


**FIG. 4.** Relative real permittivity ( $\epsilon'_{r,\text{obs}}$ ) and temperature coefficient of resonant frequency ( $\tau_f$ ) as a function of  $x$  value for  $x\text{Ca}_2\text{AlNbO}_6:(1-x)\text{Ca}_3\text{Nb}_2\text{O}_8$  compositions (Table 3). The temperature-compensated mixture occurs near  $x = 0.67$  with a corrected permittivity of  $\sim 32$ .

X-ray diffraction patterns of specimens annealed at higher temperatures show the presence of other phases. For example, in the pattern published for  $\text{Ca}_3\text{Nb}_2\text{O}_8-x$ , with indices based on a primitive tetragonal unit cell ( $a = 16.90$ ,  $c = 23.73$  Å,  $P4/nmc$ ) (33), the peak indexed as (008) at  $d = 2.9664$  Å in fact belongs to the impurity phase  $\text{Ca}_2\text{Nb}_2\text{O}_7$ . Assuming a perovskite-type structural formula  $\text{A}_3\text{B}_3\text{O}_9$ , with  $B$ -cation sites and oxygen sites fully occupied,  $\text{Ca}_3\text{Nb}_2\text{O}_8$  corresponds to  $\text{Ca}_{2.625}\square_{0.375}[\text{Ca}_{0.75}\text{Nb}_{2.25}]_9\text{O}_9$ , where “ $\square$ ” denotes  $A$ -cation vacancies. Likewise, the single-phase composition 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub> corresponds to  $\text{Ca}_{2.642}\square_{0.358}[\text{Ca}_{0.761}\text{Nb}_{2.239}]_9\text{O}_9$ , which results



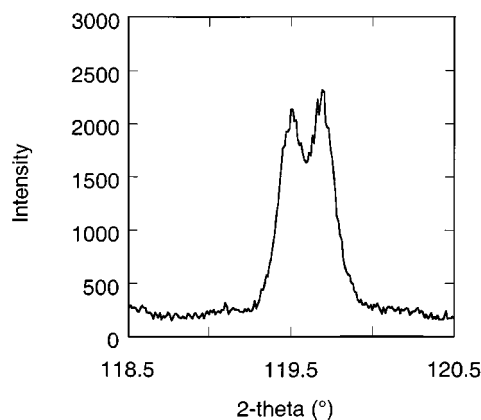
**FIG. 5.** Phase equilibria relations found in the CaO-rich portion of the CaO:Nb<sub>2</sub>O<sub>5</sub> system. The “3:1” ordered polymorph of  $\text{Ca}_4\text{Nb}_2\text{O}_9$ , described elsewhere as the metastable “ $\text{LT}_{1/4}$ ” phase (31, 32), was found to be stable at 21 mol% Nb<sub>2</sub>O<sub>5</sub> between 1375 and 1575°C. The phase referred to as  $\text{Ca}_3\text{Nb}_2\text{O}_8$  (= 75:25 CaO:Nb<sub>2</sub>O<sub>5</sub>) was found to occur with little or no solid solution at the composition 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub>.



**FIG. 6.** X-ray diffraction patterns of CaO:Nb<sub>2</sub>O<sub>5</sub> specimens near the composition Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> (= 75:25 CaO:Nb<sub>2</sub>O<sub>5</sub>), which always exhibited small amounts of the neighboring binary compound Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub>, as shown, despite extensive reannealing just below its decomposition temperature of 1475°C. The patterns are labeled according to mol% CaO. The compound referred to as Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> was found to form as a single phase at 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub>, as seen here. At CaO levels above 75.25 mol%, traces of the other neighboring compound Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub> appear in the X-ray powder diffraction pattern.

in a reduced number of cation vacancies; however, the reason that this compound forms at this particular stoichiometry is not known.

The X-ray powder diffraction data for the pure Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>-type phase (75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub>) up to  $2\theta = 70^\circ$  could be completely indexed using a face-centered



**FIG. 7.** High-angle, high-resolution X-ray powder diffraction pattern of the composition 75.25CaO:24.75Nb<sub>2</sub>O<sub>5</sub>, which contains the Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>-type compound as a single phase, showing splitting of the diffraction peak ( $h^2 + k^2 + l^2$ )<sub>(cubic)</sub> = 720. The data shown were obtained with an incident beam monochromator and a PSD detector; therefore,  $K\alpha_2$  lines are not present. This splitting indicates that the structure deviates from cubic symmetry. The detailed crystal structure of the Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>-type phase and the reason it occurs off-stoichiometry at 75.25CaO:24.75Nb<sub>2</sub>O<sub>5</sub>, as essentially a point compound, are not yet known.

cubic cell with  $a = 23.93 \text{ \AA}$ . Single-crystal X-ray precession patterns with superstructure spots showing six times the basic 4- $\text{\AA}$  perovskite unit cell were also consistent with this cubic unit cell. However, optical microscopy indicated that the crystals were weakly birefringent rather than isotropic, and showed no sign of twinning. Examination of the high-angle ( $2\theta > 70^\circ$ ) reflections in the X-ray powder diffraction data revealed that several strong peaks are split, indicating deviation from cubic symmetry. This peak splitting was especially noted for ( $h^2 + k^2 + l^2$ )<sub>(cubic)</sub> sums equal to 432, 648, 720, and 864, as shown in Fig. 7. Further characterization of this phase using synchrotron diffraction, neutron powder diffraction, electron diffraction, and single-crystal methods is in progress and will be described elsewhere.

## CONCLUSIONS

A subsolidus phase equilibria study of the CaO:Al<sub>2</sub>O<sub>3</sub>:Nb<sub>2</sub>O<sub>5</sub> system at 1325°C in air indicates the occurrence of a single ternary compound, Ca<sub>2</sub>AlNbO<sub>6</sub>, that exhibits a perovskite-related structure with 1:1 or NaCl-type ordering of Al<sup>3+</sup> and Nb<sup>5+</sup> on the B sites. The X-ray powder diffraction pattern of this compound was indexed with a monoclinic unit cell ( $P2_1/n$  (No. 11);  $a = 5.3780(1)$ ,  $b = 5.4154(1)$ ,  $c = 7.6248(2) \text{ \AA}$ ,  $\beta = 89.968(2)^\circ$ ). Capacitance methods at 1 MHz were used to determine the dielectric constant and its temperature coefficient for 11 compounds in the system; the results suggested that a stable, temperature-compensated mixture could be prepared along the Ca<sub>2</sub>AlNbO<sub>6</sub>-Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> composition line. Dielectric resonator methods at 5–7 GHz were used to determine the properties of 5 compositions in the  $x\text{Ca}_2\text{AlNbO}_6 \cdot (1-x)\text{Ca}_3\text{Nb}_2\text{O}_8$  system; temperature compensation of the resonant frequency was obtained near  $x = 0.67$  with a permittivity of 32. No solid solution between Ca<sub>2</sub>AlNbO<sub>6</sub> and Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub> was observed. The system CaO-Nb<sub>2</sub>O<sub>5</sub> was reexamined at CaO contents above 70 mol% to clarify conflicting information in the literature. Two phases were confirmed to form in this region: the polymorphic-ordered perovskite Ca<sub>4</sub>Nb<sub>2</sub>O<sub>9</sub>, with solid solution ranging from approximately 17 to 20.5 mol% Nb<sub>2</sub>O<sub>5</sub>, and the compound referred to as Ca<sub>3</sub>Nb<sub>2</sub>O<sub>8</sub>, which was shown here to occur as essentially a point compound at the composition 75.25:24.75 CaO:Nb<sub>2</sub>O<sub>5</sub>. Structural characterization indicated that this phase is a defect perovskite with a noncubic unit cell; however, the detailed crystal structure and the reason it forms at this particular stoichiometry are not yet known.

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